

The Orthorhombic Structure of Y_3Co_2 , a Shift Structure Variation of the Monoclinic Dy_3Ni_2 Type

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Y_3Co_2 crystallizes with a new orthorhombic structure type. Space group $Pnmm$ (No. 58); $a=12.248$, $b=9.389$, $c=3.975$ Å; $Z=4$, $D_x=5.58$ g cm $^{-3}$, F.W. 384.58, $F(000)=684$, $\mu(Mo K\alpha)=426$ cm $^{-1}$, $R=0.10$. The structures of Y_3Co_2 and the earlier determined Dy_3Ni_2 are shift structure variants. Both structures are characterized by infinite bands formed by joining four infinite trigonal prism columns. The arrangement of these bands is, however, different in the two structure types. Slicing one of the structure types in blocks of equal size and shifting them with respect to one another leads to an atom arrangement characteristic of the other structure type.

Introduction

The published data for the binary phase diagram of Y and Co near 37 at. % Co is contradictory.

Buschow (1971) reported the existence of a phase Ln_xCo with 37 at. % Co for $Ln=Gd, Dy, Ho, Er$ and Y. Schweizer (1972) determined the structure of $Ho_{12}Co_7$ (monoclinic, $P2_1/b$, $a=9.30$, $b=13.85$, $c=11.16$ Å, $\beta=144^\circ$) which composition corresponds to 37 at. % Co. Ray (1974) published a phase diagram of the Y-Co system due to Strnat, Ostertag, Adams & Olson (1965) in which the Y_xCo phase mentioned by Buschow does not appear. Thermoanalytical and metallographic examinations do not give a stoichiometry as precise as do single-crystal X-ray structure determinations.

The purpose of this paper is to present the results of our single-crystal structure determination for this phase of which the composition is Y_3Co_2 or 40 at. % Co.

Experimental

Yttrium of 99.9% and cobalt of 99.99% purity were used to prepare the samples studied in this investigation. The constituents in proportions ranging from 35 to 40 at. % Co were induction-melted in an alumina crucible under argon atmosphere. Needle-shaped single crystals were directly isolated from the crushed melt. Preliminary Weissenberg and precession photographs showed the crystals to be orthorhombic with space group $Pnmm$ or $Pnn2$. Lattice constants and intensities were measured with graphite-monochromated $Mo K\alpha$ radiation and a Philips PW 1100 computer-controlled four-circle goniometer. The cell parameters are: $a=12.248$ (8), $b=9.389$ (6) and $c=3.975$ (3) Å.

The intensities of 190 non-equivalent observed

reflexions ($I > 2\sigma$) were recorded out to a limit of 0.7 \AA^{-1} and all were used in the structure determination (see Table 1).

Table 1. Observed and calculated structure factors for Y_3Co_2

Reading from left to right the columns contain the values $h, k, l, |F_o|$ and $|F_c|$.

4	0	0	259	237	2	2	1	56	23	14	6	2	103	106
5	0	0	298	265	6	2	1	129	110	6	3	2	97	102
10	0	0	82	74	10	2	1	208	234	1	13	2	120	130
12	0	0	210	194	9	3	1	176	161	3	13	2	106	107
6	1	0	142	113	1	3	1	139	132	4	13	2	113	70
6	1	0	110	102	4	3	1	60	48	3	0	3	110	111
10	1	0	87	63	9	3	1	180	153	7	0	3	276	151
11	1	0	119	112	10	3	1	33	34	15	0	3	92	100
12	1	0	73	57	13	3	1	85	93	4	1	3	160	151
13	1	0	73	61	1	4	1	172	155	3	1	3	110	112
5	2	0	261	234	9	4	1	100	99	5	1	3	91	92
13	2	0	102	104	15	4	1	43	65	7	1	3	236	263
17	2	0	115	123	3	5	1	146	154	2	2	3	93	92
1	3	0	106	101	3	5	1	163	151	6	2	3	118	106
2	3	0	237	221	4	5	1	206	262	10	2	3	152	155
3	3	0	173	154	5	5	1	101	103	1	3	3	88	89
5	3	0	225	135	7	5	1	101	79	0	0	3	121	120
7	3	0	153	147	0	5	1	160	167	1	3	3	88	89
9	3	0	99	80	16	5	1	136	67	1	4	3	102	106
10	3	0	91	60	4	6	1	62	63	9	4	3	121	120
14	3	0	35	66	6	6	1	136	93	3	5	3	108	113
15	3	0	151	84	16	6	1	129	113	0	5	3	115	113
0	4	0	306	290	10	7	1	96	97	1	6	3	79	81
6	4	0	43	70	1	6	1	211	202	5	5	3	118	136
12	4	0	90	77	3	7	1	122	127	4	7	3	95	133
1	5	0	121	125	5	6	1	68	100	6	6	3	76	74
3	5	0	67	53	6	6	1	76	50	9	7	3	88	63
7	5	0	76	63	7	6	1	105	95	1	8	3	144	161
11	5	0	148	148	9	5	1	107	108	1	9	3	75	64
12	5	0	120	112	1	11	1	40	96	3	5	3	91	104
14	5	0	56	49	4	11	1	92	99	5	5	3	76	83
1	6	0	228	215	5	11	1	115	114	11	6	3	99	115
3	6	0	151	135	0	0	2	176	162	1	11	3	94	80
9	6	0	96	107	4	0	2	182	151	0	0	4	206	160
9	0	0	125	130	8	0	2	244	233	4	0	4	106	134
11	0	0	70	134	12	0	2	180	173	8	0	4	161	166
2	7	0	137	105	5	1	2	93	91	12	0	4	124	110
3	7	0	61	67	6	1	2	92	85	5	2	4	121	122
5	7	0	62	96	11	1	2	66	98	1	3	4	111	50
6	7	0	169	163	5	2	2	200	153	1	3	4	115	122
7	7	0	38	83	13	2	2	36	36	5	3	4	112	110
8	0	0	138	115	17	2	2	116	115	6	3	4	163	162
6	9	0	36	67	1	3	2	77	61	0	4	4	156	153
8	9	0	72	47	2	3	2	179	175	8	4	4	72	63
14	0	0	104	114	3	3	2	127	124	12	0	4	124	110
17	0	0	84	24	5	3	2	171	161	0	4	4	156	153
5	9	0	99	111	6	3	2	246	234	12	0	4	72	62
5	9	0	91	64	7	3	2	130	125	11	0	4	105	100
9	10	0	153	148	0	4	2	98	102	11	0	4	123	130
3	10	0	151	108	4	4	2	102	117	7	0	4	109	113
5	10	0	106	52	12	4	2	68	69	5	7	4	96	63
9	10	0	10	110	14	4	2	122	96	10	2	5	125	129
0	12	0	103	79	1	5	2	114	105	0	5	5	71	63
7	12	0	31	63	10	5	2	89	73	0	0	6	146	167
1	13	0	102	117	10	5	2	101	112	0	0	6	123	130
7	13	0	101	70	11	5	2	140	132	4	0	6	149	105
3	13	0	186	167	12	5	2	122	101	5	1	6	91	71
5	13	0	103	94	1	6	2	155	165	8	0	6	146	166
7	13	0	231	200	7	6	2	196	113	4	0	6	149	105
15	1	1	163	167	7	7	2	132	96	6	0	6	124	127
5	1	1	158	147	9	6	2	123	121	0	6	6	146	166
4	1	1	252	213	2	7	2	114	96	9	1	6	91	71
5	1	1	162	152	4	7	2	81	84	6	0	6	146	166
7	1	1	130	122	5	7	2	93	95	0	6	6	128	143
6	1	1	46	60	6	6	2	127	133	0	6	6	146	166

The preparation of this phase with 40 at. % Co is not straightforward. In an induction furnace with slow cooling, this phase (I) was obtained with an initial

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stoichiometry of 37 at. % Co. With samples containing an initial 40 at. % Co another phase (II) appears which is neither Y_4Co_3 (Lemaire, Schweizer & Yakinthos, 1969) nor isotypic with $Ho_{12}Co_7$ (Schweizer, 1972). In an arc furnace, only the second phase (II), yet unidentified, was obtained. In the arc-melting technique the sample is quenched, so it may be concluded that Y_3Co_2 is a low-temperature phase and that the unknown phase (II) contains about 40 at. % Co. For verification, a sample of the low-temperature phase, obtained by induction melting and well characterized by a Guinier photograph, was arc melted. It was found that phase I disappears completely and the Guinier film only shows the lines corresponding to phase II.

Structure determination

The volume of the cell together with the space-group restrictions indicates that there are four formula units of Y_3Co_2 per cell. A Patterson map showed peaks only on the $P(x, y, 0)$ and $P(x, y, \frac{1}{2})$ sections. This observation is due to the fact that the c parameter is so small that atoms can only be located on planes at $z=0$ or $z=\frac{1}{2}$ assuming the centrosymmetric space group $Pnmm$.

From the location of Patterson peaks various trial structures could be postulated for the 12Y atoms alone. However, only one of these models refined satisfactorily with the program *STEPRF* (X-RAY System, 1972). From an electron-density map it was possible to place eight Co atoms in two different sites. All positional and isotropic thermal parameters refined satisfactorily with the least-squares program *CRYLSQ* (X-RAY

system, 1972). Hartree-Fock scattering factors were used. No anomalous dispersion and absorption corrections were considered.

The R ($\sum|\Delta F|/\sum|F_o|$) index calculated with 190 observed reflexions was 0.10. The final positional and thermal parameters are listed in Table 2. Coordination distances are given in Table 3. As this structure is of a new type a listing of the low-angle reflexions with corresponding intensities for X-ray powder diagram identification is given in Table 4.

Table 2. *Least-squares atomic parameters for Y_3Co_2 with e.s.d.'s in parentheses*

Isotropic temperature factor is $\exp[-2\pi^2 \times 10^{-2} U(2 \sin \theta/\lambda)^2]$.
Space group $Pnmm$. All atoms in equipoint $4(g)$.

	x	y	z	U (\AA^2)
Y(1)	0.128 (1)	0.193 (1)	0	0.7 (3)
Y(2)	0.387 (1)	0.373 (2)	0	0.6 (3)
Y(3)	0.137 (1)	0.574 (2)	0	0.6 (3)
Co(1)	0.269 (2)	0.860 (2)	0	0.3 (4)
Co(2)	0.462 (2)	0.883 (3)	0	0.8 (4)

Discussion

A projection of the Y_3Co_2 structure along the short c axis is shown on the left-hand side of Fig. 1. Four columns of Co-centered trigonal rare-earth prisms are joined to form a band. The complete structure consists of such four-column bands aligned parallel to c . The same structural features are found in the structure of Dy_3Ni_2 (Moreau, Paccard & Parthé, 1974), shown on the right-hand side of Fig. 1.

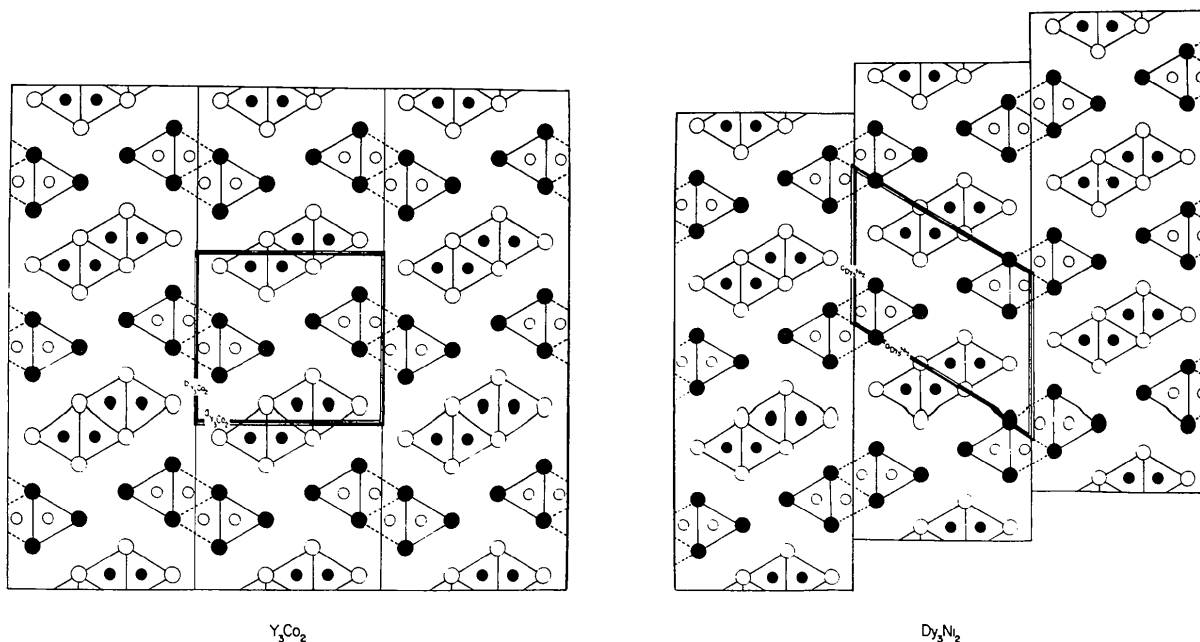


Fig. 1. Projections of orthorhombic Y_3Co_2 along c and monoclinic Dy_3Ni_2 along b . Full black circles in 0 and white circles in $\frac{1}{2}$. Large circles represent Y or Dy and small circles Co or Ni atoms. Dy_3Ni_2 can be derived from Y_3Co_2 by shifting slabs common to both structures.

Table 3. *Coordination distances in Y₃Co₂ (Å)*

Y(1)-2Co(1)	2.83	Y(3)-2Co(2)	2.94
2Co(2)	2.89	2Co(2)	2.95
Y(3)	3.57	2Co(1)	3.05
Co(1)	3.57	Co(1)	3.14
Y(2)	3.59	2Y(2)	3.45
2Y(2)	3.60	Y(1)	3.57
2Y(2)	3.61	Y(2)	3.59
2Y(3)	3.67	Y(3)	3.63
		2Y(1)	3.67
Y(2)-2Co(1)	2.76	Co(1)-Co(2)	2.37
Co(2)	3.03	2Y(2)	2.76
2Y(3)	3.45	2Y(1)	2.83
Y(1)	3.59	2Y(3)	3.05
Y(3)	3.59	Y(3)	3.14
2Y(1)	3.60	Y(1)	3.57
2Y(1)	3.61		
Y(2)	3.65		
		Co(2)-Co(1)	2.37
		Co(2)	2.39
		2Y(1)	2.89
		2Y(3)	2.94
		2Y(3)	2.95
		Y(2)	3.03

Table 4. *Calculated powder data for Y₃Co₂ for Cr K α radiation ($\lambda = 2.29092 \text{ \AA}$)*

Intensity data calculated with point positions obtained from single-crystal data. $I = mF^2(1 + \cos^2 2\theta)/\sin^2 \theta$, $\cos \theta$ is normalized to the strongest reflexion having intensity 1000.

<i>h k l</i>	$\sin^2 \theta$	Intensity	<i>h k l</i>	$\sin^2 \theta$	Intensity
1 1 0	23.63	68.2	0 3 1	217.08	80.5
2 0 0	34.99	3.7	3 2 1	221.38	2.5
2 1 0	49.87	2.1	1 3 1	225.83	53.8
0 2 0	59.54	0.1	5 1 0	233.54	35.9
1 2 0	68.28	3.9	4 1 1	237.95	187.2
1 0 1	91.87	5.2	0 4 0	238.14	138.9
3 1 0	93.60	2.9	1 4 0	246.89	1.1
2 2 0	94.52	5.1	2 3 1	252.07	41.4
0 1 1	98.01	4.3	2 4 0	273.13	0.3
1 1 1	106.75	10.2	4 3 0	273.90	5.1
2 1 1	132.99	0.2	5 2 0	278.20	151.6
3 2 0	138.25	0.0	4 2 1	282.60	0.0
4 0 0	139.94	140.4	3 3 1	295.80	0.0
1 3 0	142.70	29.9	5 0 1	301.78	7.0
1 2 1	151.41	4.1	6 0 0	314.87	0.7
4 1 0	154.83	2.4	5 1 1	316.67	90.5
3 0 1	161.84	124.5	3 4 0	316.86	0.4
2 3 0	168.94	100.1	6 1 0	329.75	18.4
3 1 1	176.72	125.9	1 4 1	330.01	64.8
2 2 1	177.65	1000.0	0 0 2	332.49	190.8
4 2 0	199.48	0.7	5 3 0	352.62	43.6
3 3 0	212.67	110.2			

The Y₃Co₂ and Dy₃Ni₂ structure types are shift structure variants and are geometrically related in similar fashion to the CrB, FeB and TbNi (Hohnke & Parthé, 1966; Lemaire & Paccard, 1970), or the AlB₂ and ThSi₂ (Parthé, 1967) or the CeAl and DyAl structure types (Bècle & Lemaire, 1967).

To demonstrate the geometrical relationship between the two types it is useful to consider idealized

structure types where the basis planes of the trigonal prisms are equilateral triangles of length g . The relative cell dimensions and atom positions of the idealized Y₃Co₂ and the idealized Dy₃Ni₂ structure type are given in Table 5. Consider two neighbouring idealized Y₃Co₂ unit cells with a common (100) face. As shown in Fig. 1, a shift of one cell by g in the b direction leads to the same atom arrangement as in the idealized monoclinic Dy₃Ni₂ structure type.

Table 5. *Theoretical structure data for the idealized Y₃Co₂ and Dy₃Ni₂ structure types*

Y ₃ Co ₂	Dy ₃ Ni ₂
<i>Pnmm</i>	<i>C2/m</i>
$a = 2\sqrt{3}g$	$a = 4g$
$b = 3g$	$b = \text{free, same as } c_{Y_3Co_2}$
$c = \text{free, same as } b_{Dy_3Ni_2}$	$c = 3g$
	$\beta = 120^\circ$

In the idealized structure types the trigonal prisms have an equilateral triangle as base where g is the length of the triangle side.

All atoms in 4(<i>g</i>)			All atoms in 4(<i>i</i>)				
	<i>x</i>	<i>y</i>	<i>z</i>	<i>x</i>	<i>y</i>	<i>z</i>	
Y(1)	$\frac{\sqrt{3}}{4} \frac{g}{a} = \frac{1}{8}$	$\frac{3g}{4b} = \frac{1}{4}$	0	Dy(1)	$\frac{1g}{2a} = \frac{1}{8}$	0	0
Y(2)	$\frac{3\sqrt{3}}{4} \frac{g}{a} = \frac{3}{8}$	$\frac{5g}{4b} = \frac{5}{12}$	0	Dy(2)	$\frac{3g}{2a} = \frac{3}{8}$	0	$\frac{1g}{c} = \frac{1}{3}$
Y(3)	$\frac{\sqrt{3}}{4} \frac{g}{a} = \frac{1}{8}$	$\frac{7g}{4b} = \frac{7}{12}$	0	Dy(3)	$\frac{1g}{2a} = \frac{1}{8}$	0	$\frac{1g}{c} = \frac{1}{3}$
Co(1)	$\frac{7\sqrt{3}}{12} \frac{g}{a} = \frac{7}{24}$	$\frac{11g}{4b} = \frac{11}{12}$	0	Ni(1)	$\frac{13g}{6a} = \frac{13}{24}$	0	$\frac{1g}{3c} = \frac{1}{9}$
Co(2)	$\frac{11\sqrt{3}}{12} \frac{g}{a} = \frac{11}{24}$	$\frac{11g}{4b} = \frac{11}{12}$	0	Ni(2)	$\frac{17g}{6a} = \frac{17}{24}$	0	$\frac{2g}{3c} = \frac{2}{9}$

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